

Weighing up the options:  
Finding the right solution when  
lots of things matter

Sandy Brownlee

# Outline

- Decision making, multiple objectives
- Optimisation
- Building design
- Evolutionary algorithms
- Other real world applications

Showing 1 - 20 of 90 results

Sort by ▼

- Relevance
- Please select
- Relevance**
- Brand - A to Z
- Brand - Z to A
- Price - low to high
- Price - high to low
- Customer rating

Show 20

Compare items (Up to 4 products)

1



### RUSSELL HOBBS Windsor 22832 4-Slice Toaster - Black

>

3 year guarantee included

- Defrost function
- Warming function
- Extra-wide slots

★★★★★ 852 reviews

Brief product description

£2

- ✓ FREE delivery available
- ✓ FREE collect in store available

2



### BREVILLE Impressions VTT702 4-Slice Toaster - Vanilla Cream

- Defrost function
- Extra-wide slots
- High-lift eject

★★★★★ 10 reviews

Brief product description

**£34.99** Save **£35.00**

Was £69.99 (from 31/12/15 to 20/01/16)

- ✓ FREE delivery available
- ✓ FREE collect in store available

3



### BREVILLE Impressions VTT476 4-Slice Toaster - Black

- Defrost function
- Warming function
- Extra-wide slots
- High-lift eject
- Bagel function

**£34.99** Save **£35.00**

Was £69.99 (from 31/12/15 to 22/01/16)

- ✓ FREE delivery available

Showing 1 - 20 of 90 results

Sort by Price - low to high

Show 20 products per page

Compare items (Up to 4 products)

Show [Grid icon]

1	<input type="checkbox"/> 	<p><b>ESSENTIALS C02TW13 2-Slice Toaster - White</b></p> <p>★★★★★ 30 reviews</p> <p><a href="#">Brief product description</a></p>	<p><b>£4.49</b></p> <ul style="list-style-type: none"> <li>✓ FREE delivery available</li> <li>✓ FREE collect in store available</li> </ul>
2	<input type="checkbox"/> 	<p><b>LOGIK L02TBS13 2-Slice Toaster - Stainless Steel</b></p> <ul style="list-style-type: none"> <li>• Defrost function</li> <li>• Warming function</li> <li>• Extra-wide slots</li> <li>• High-lift eject</li> </ul> <p>★★★★★ 43 reviews</p> <p><a href="#">Brief product description</a></p>	<p><b>£12.49</b></p> <ul style="list-style-type: none"> <li>✓ FREE delivery available</li> <li>✓ FREE collect in store available</li> </ul>
3	<input type="checkbox"/> 	<p><b>BREVILLE VTT375 2-Slice Toaster - Polished Stainless Steel</b></p> <ul style="list-style-type: none"> <li>• Defrost function</li> <li>• Warming function</li> <li>• Extra-wide slots</li> <li>• High-lift eject</li> </ul>	<p><b>£16.99</b></p> <ul style="list-style-type: none"> <li>✓ FREE delivery available</li> <li>✓ FREE collect in store available</li> </ul>

Showing 1 - 20 of 90 results

Sort by Price - high to low

Show 20 products per page

Compare items (Up to 4 products)

Show [Grid icon]

1



### KITCHENAID 5KMT4205BMS Artisan 4-Slice Toaster - Silver

- Defrost function
- Warming function

★★★★★ 3 reviews

[Brief product description](#)

£269.99

- ✓ FREE delivery available
- ✓ FREE collect in store available

2



### KITCHENAID 5KMT4205BER Artisan 4-Slice Toaster - Empire Red

- Defrost function
- Warming function
- Extra-wide slots
- Bagel function

★★★★★ 3 reviews

[Brief product description](#)

£269.99

- ✗ Sorry this item is out of stock
- ✉ [Email me when back in stock](#)

3



### MORPHY RICHARDS Redefine 228000 2-Slice Toaster - Glass

2 year guarantee included

- Defrost function

£199.99

- ✓ FREE delivery available
- ✓ FREE collect in store available



Stirling, UK

Banff, Aberdeenshire, UK

Route options CLOSE

Avoid

- Highways
- Tolls
- Ferries

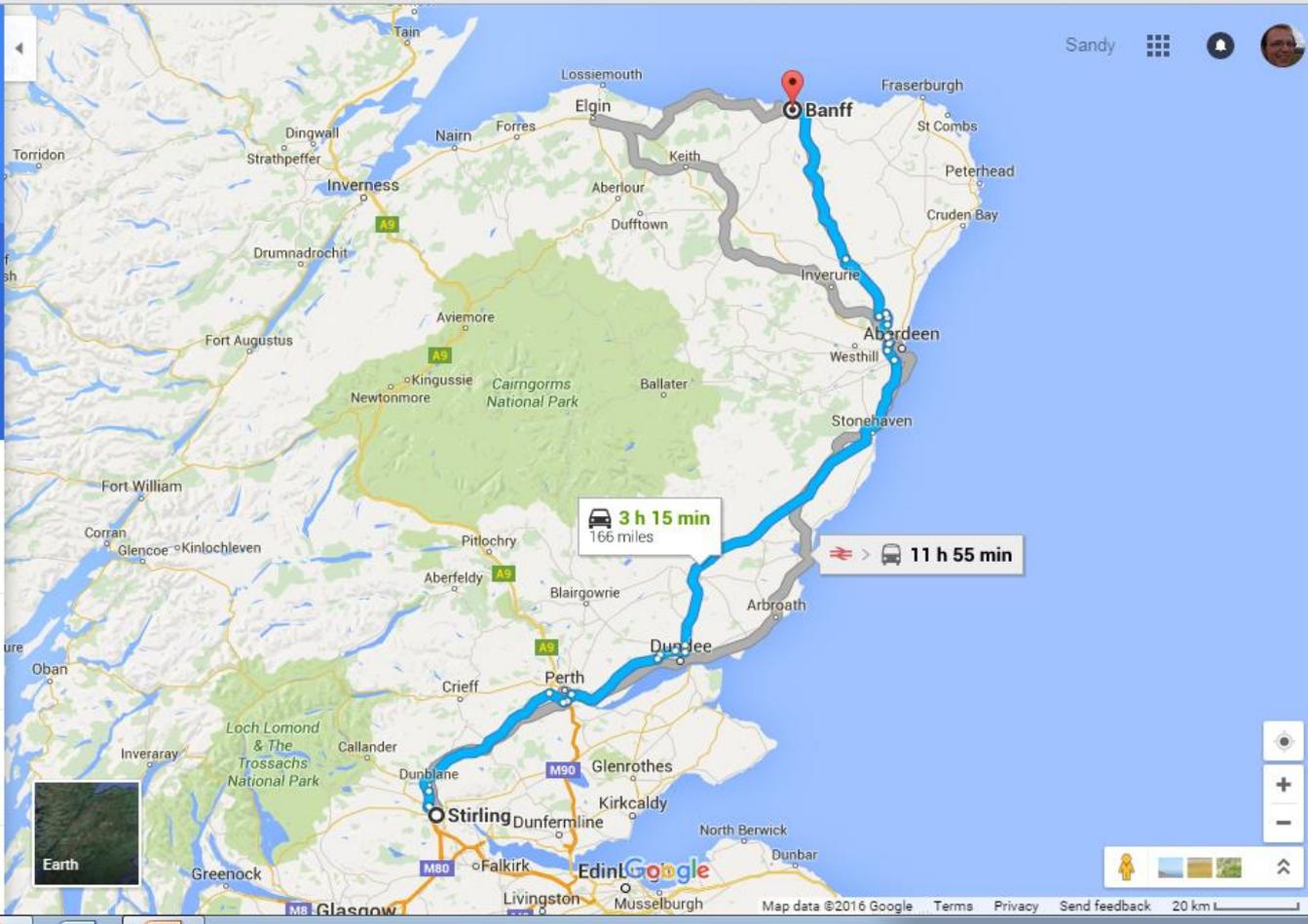
Distance units

- Automatic
- miles
- km

via A90 **3 h 15 min**  
 3 h 7 min without traffic 166 miles  
[DETAILS](#)

10:07 PM–9:53 AM 11 h 46 min  
 ScotRail > ScotRail > 35

10:07 PM–10:02 AM 11 h 55 min  
 ScotRail > 35



Travel > News & Advice

# Teenager flies from Sheffield to Essex via Berlin because it is cheaper than getting the train

Jordan Cox said the 1,017 mile round trip to Germany was £7.72 cheaper than a direct train home

Caroline Mortimer | @cmortimer | Wednesday 27 January 2016 | 5 Comments








Jordan Cox outside the Brandenburg Gate in Berlin as he details how he saved money on his adventure Jordan Cox/YouTube

A cost-conscious teenager found the perfect way to save on his journey home - by booking a flight via Berlin.

Jordan Cox, 18, realised it would cost him £50 to travel from Sheffield to Shenfield in Essex by train but if he "went the extra 1,017 miles" he could fly via the German capital and save £7.72.

- So what if we care about more than one thing?
- More than one *objective*?

£££



Cost



£



Time for 0-60 mph





Image source: <https://commons.wikimedia.org>

- Vilfredo Pareto
  - 1848 - 1923
  - Italian engineer, sociologist, economist, political scientist, and philosopher
- *Pareto optimal front:*
  - *The trade-off of optimal designs / options / solutions*

£££



Cost



£



Time for 0-60 mph

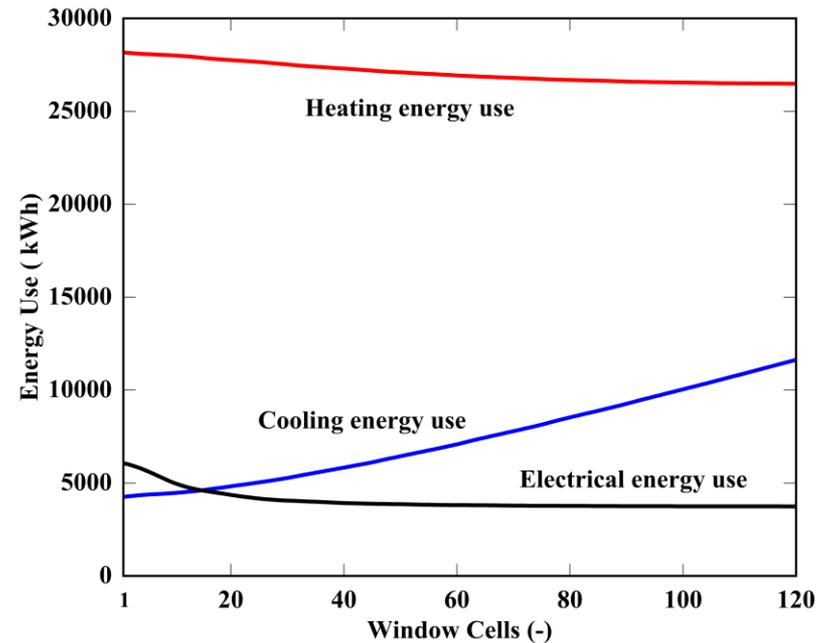
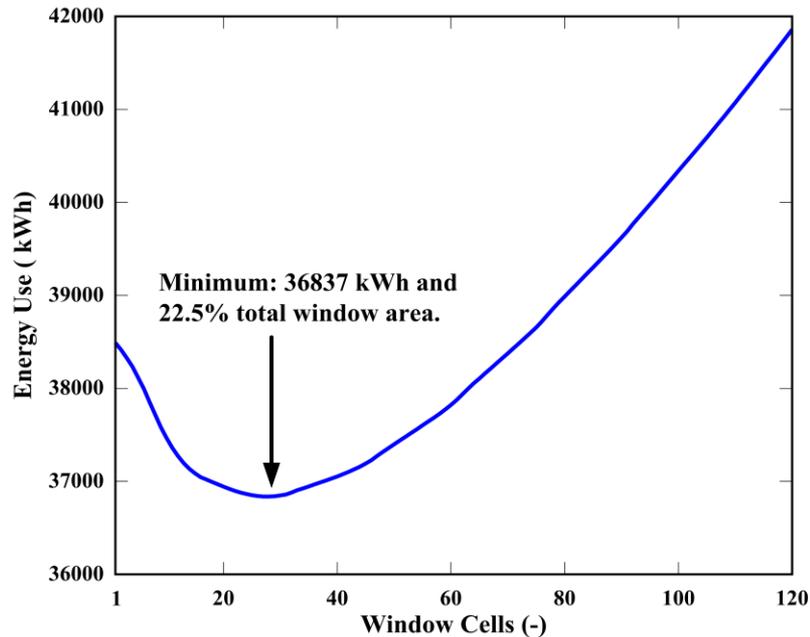
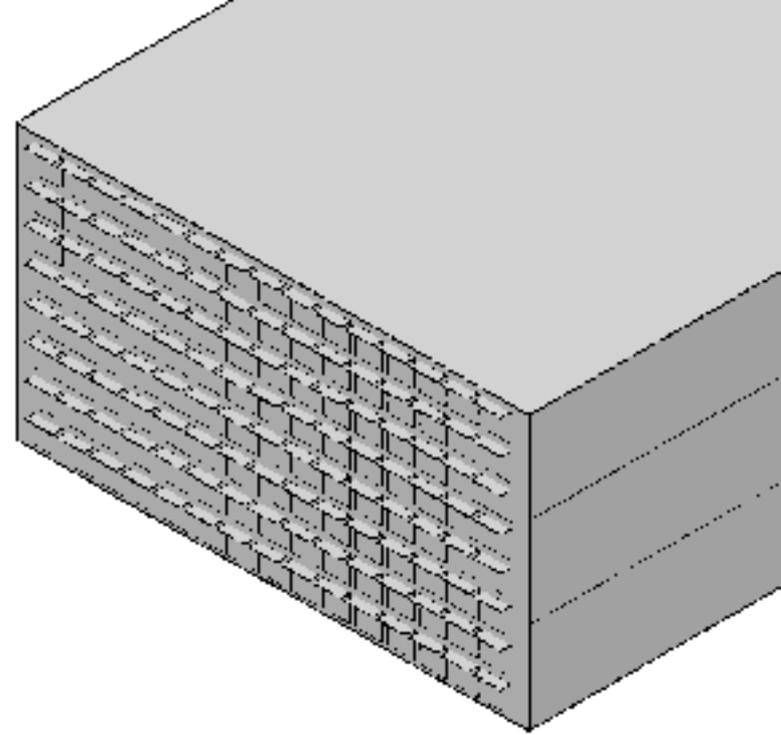


# Optimisation



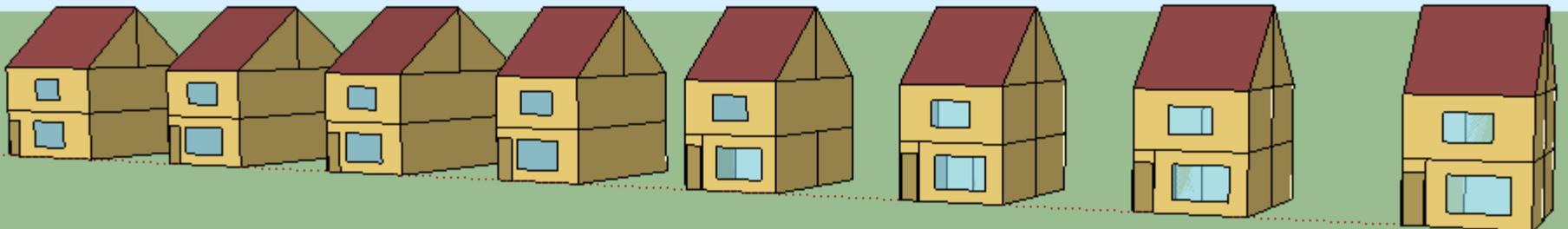
# Single-objective

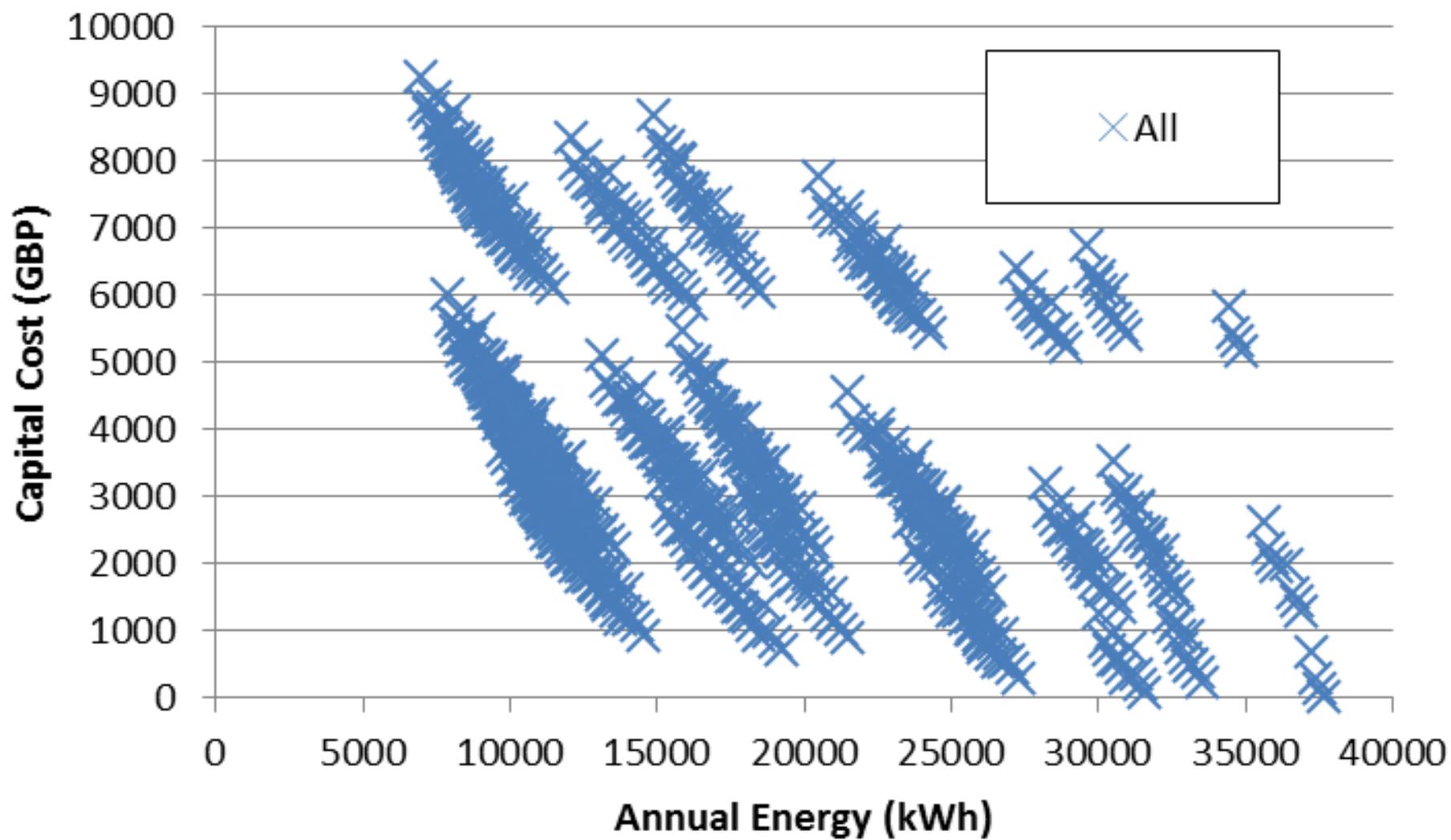
- Minimal cost easy
- Minimal energy tricky!

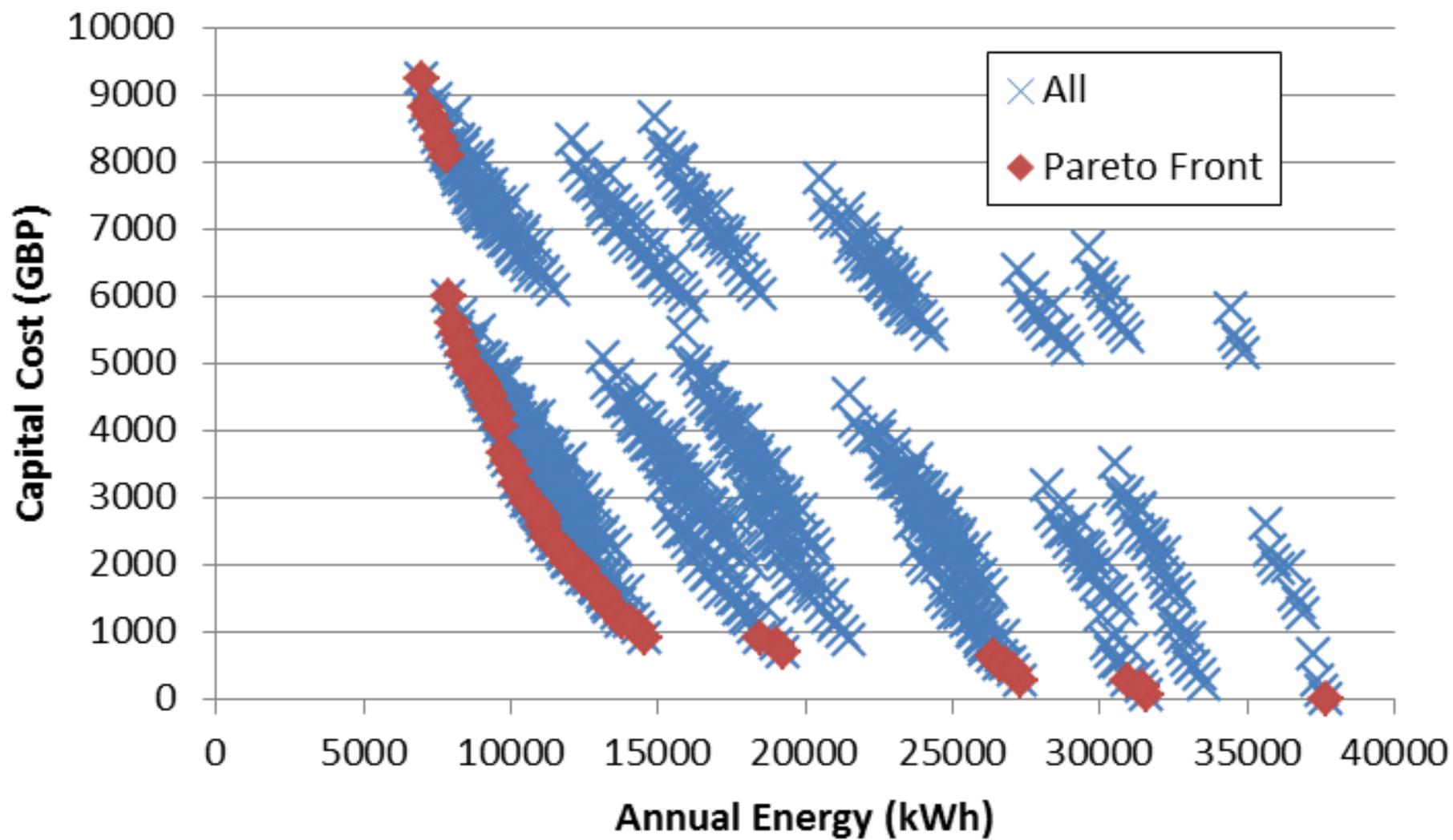


# Multi-objective

- Minimise **cost** to improve house, and the **energy** required to run it
- 5 things to vary, 4 levels each
  - Wall insulation
  - Replace windows
  - Replace door
  - Floor insulation
  - Roof insulation
- How many possible variations?







# Exhaustive search

- 5 variables, 4 values each:

$$4^5 = 4 \times 4 \times 4 \times 4 \times 4 = 1,024$$

- 10 variables:

$$4^{10} = 1,048,576$$

- 50 variables:

$$4^{50} = 1,267,650,600,228,229,401,496,703,205,376$$

or about  $10^{30}$

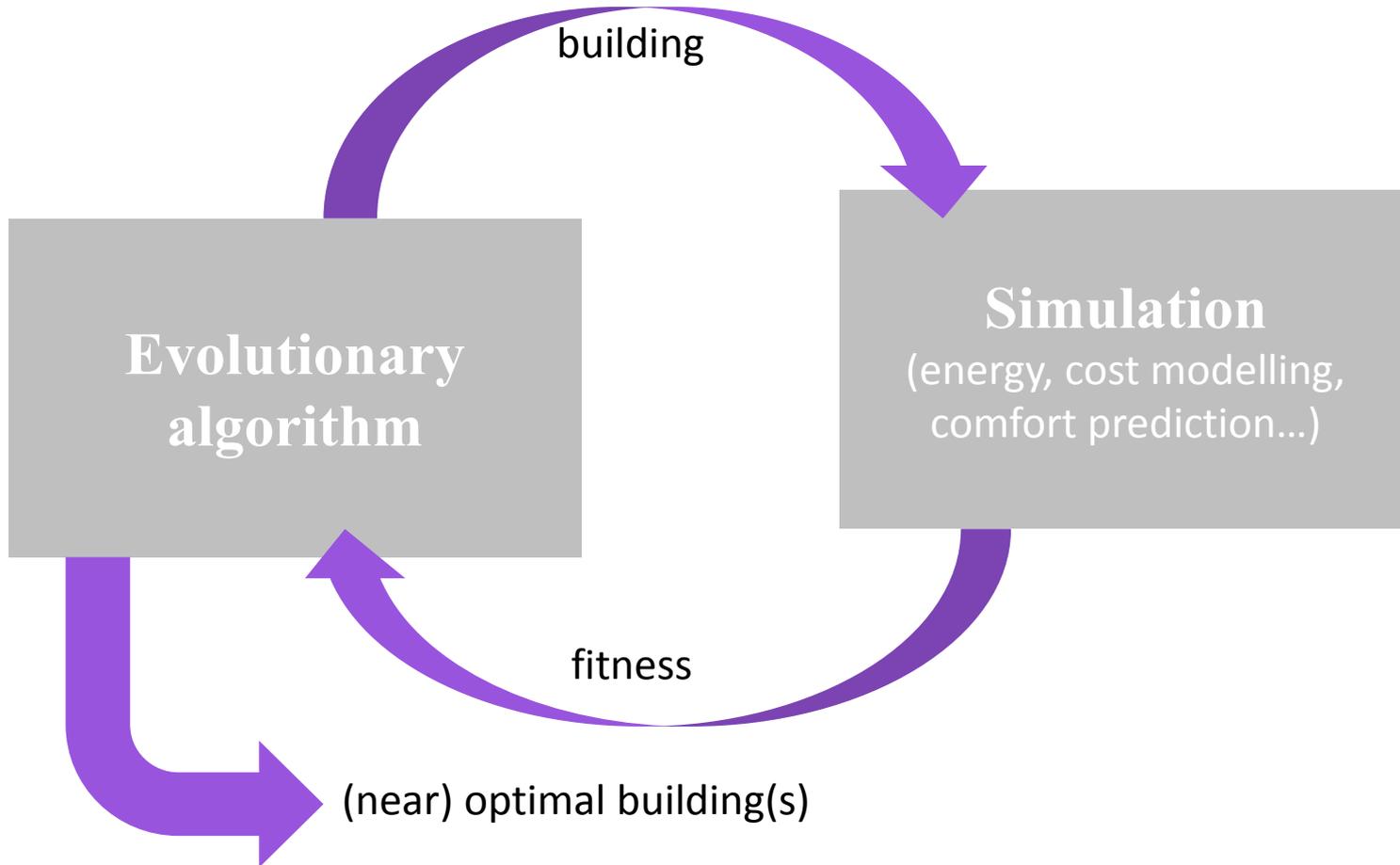
- *Combinatorial explosion*

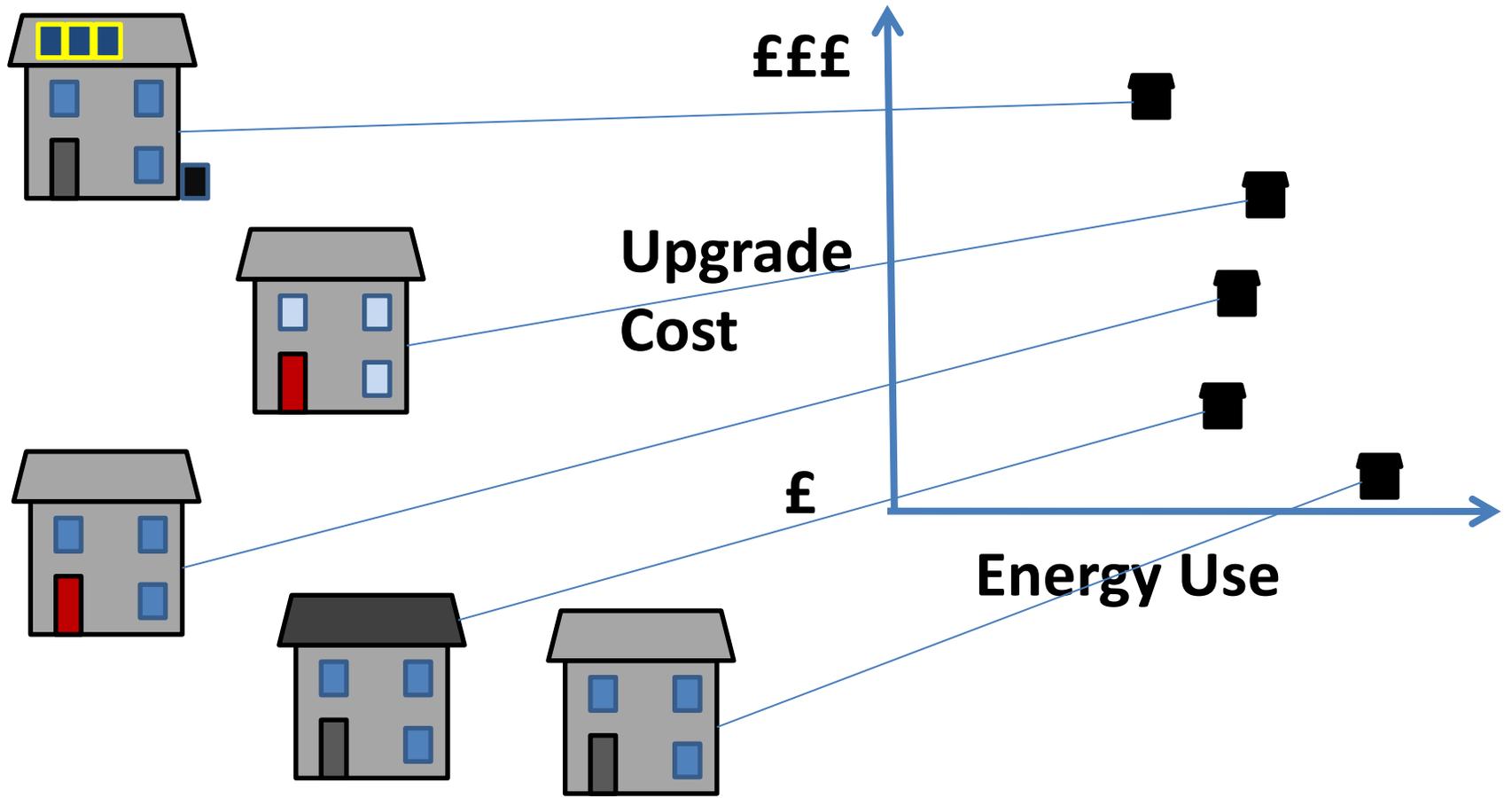
# Evolutionary algorithms

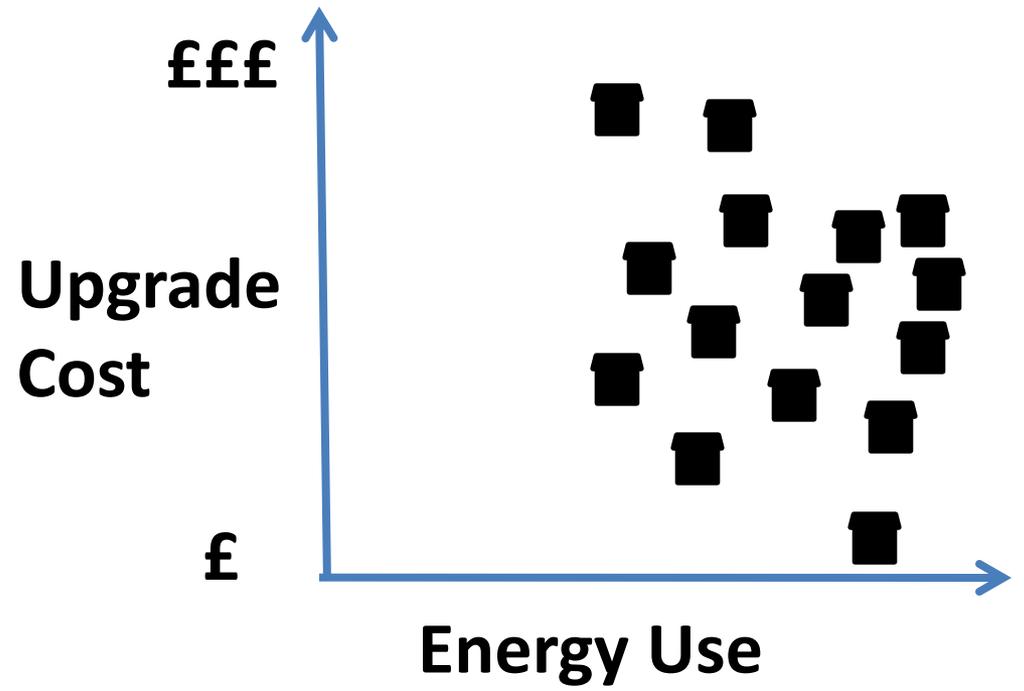
- Survival of the fittest
- Inheritance from parents to offspring

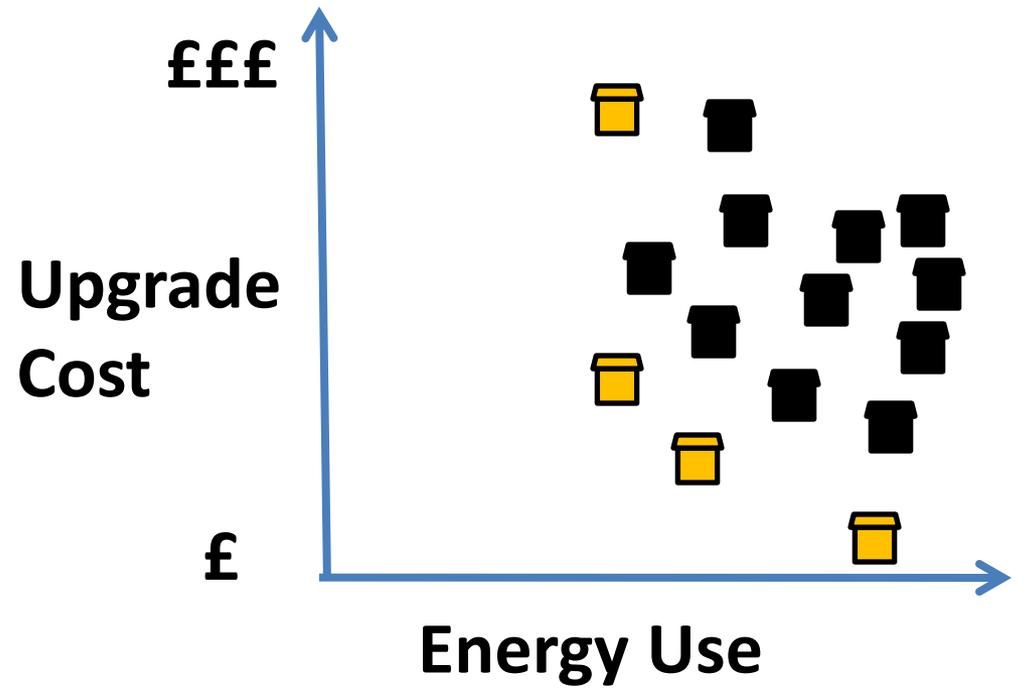


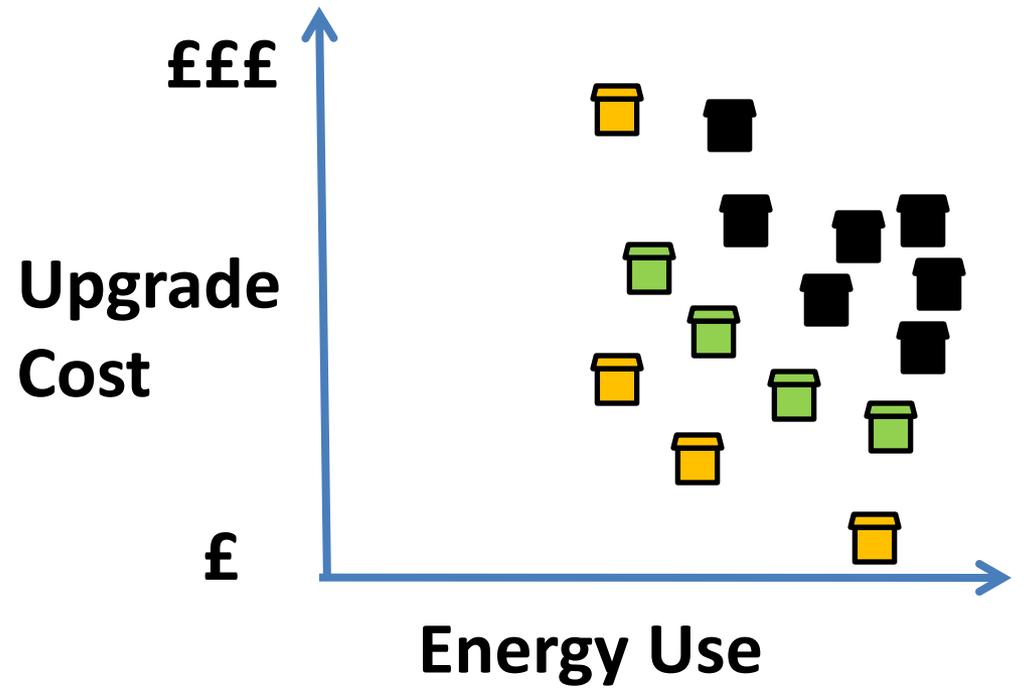
# EAs for optimising buildings

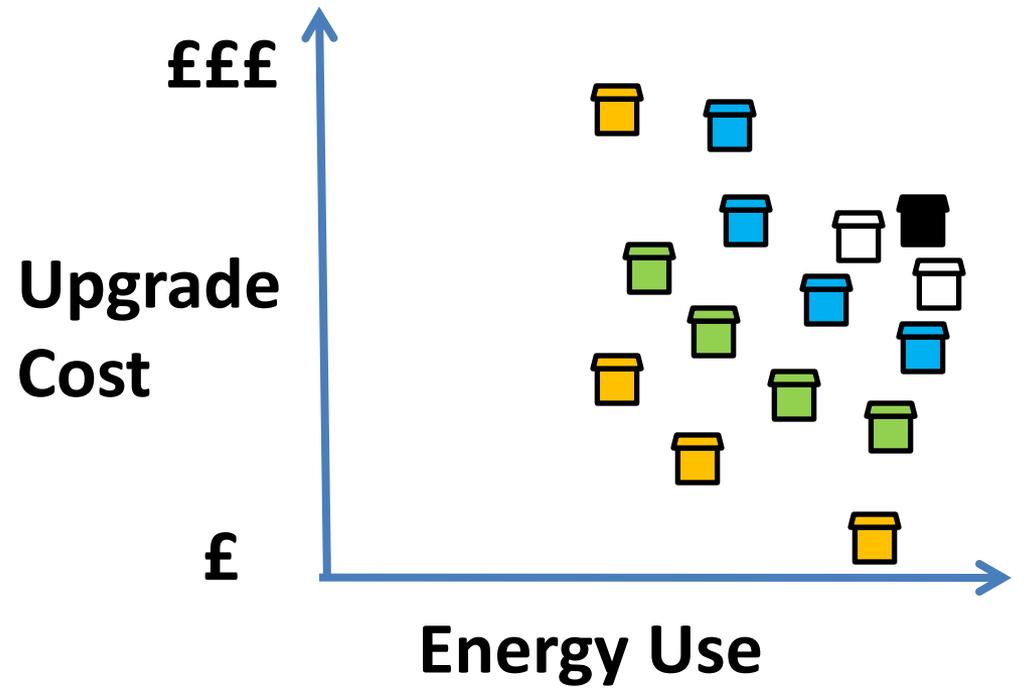


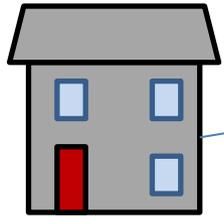












Upgrade  
Cost

£££

£

Energy Use

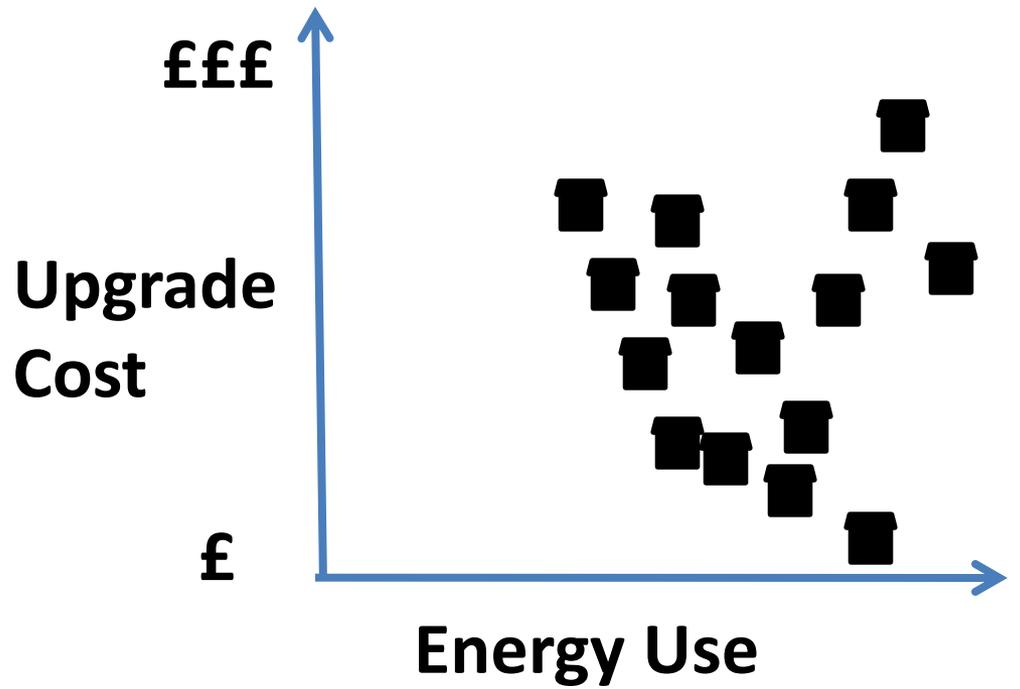
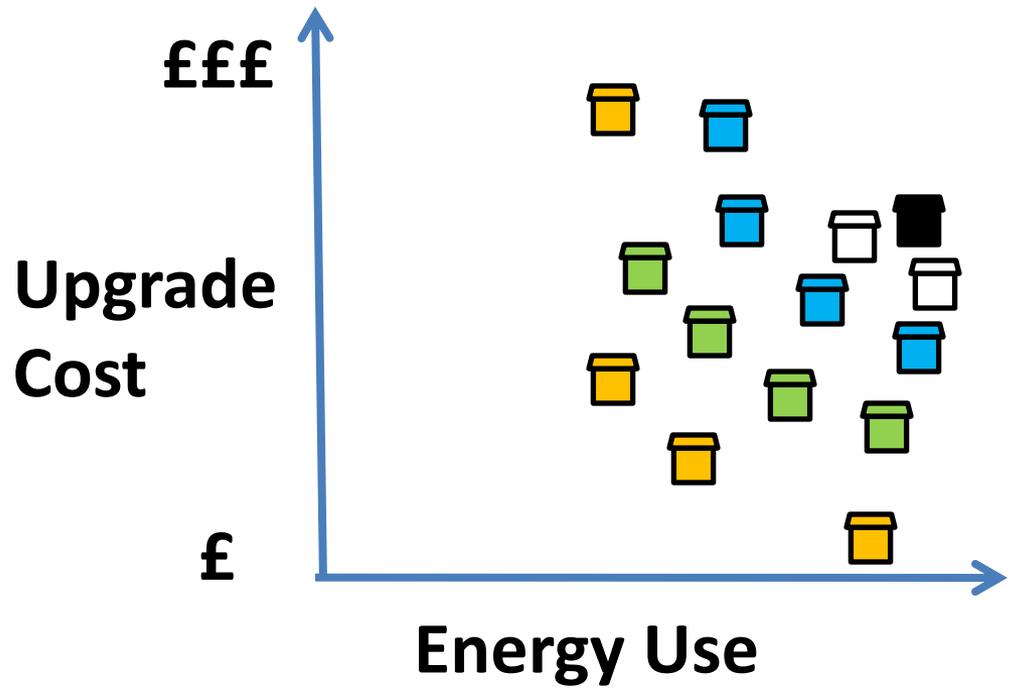
£££

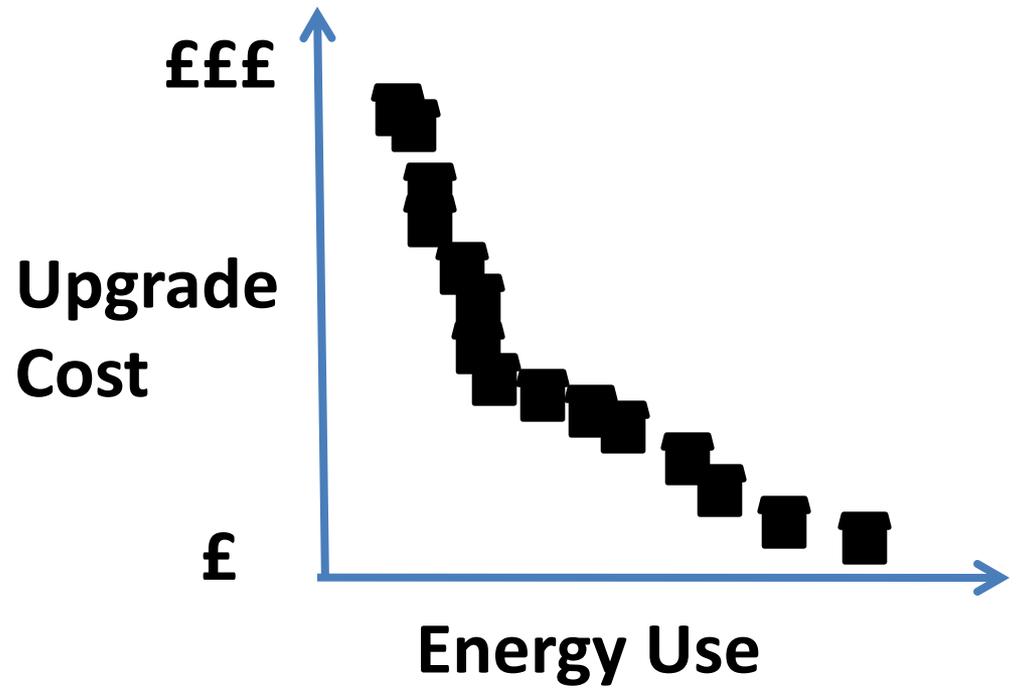
Upgrade  
Cost

£

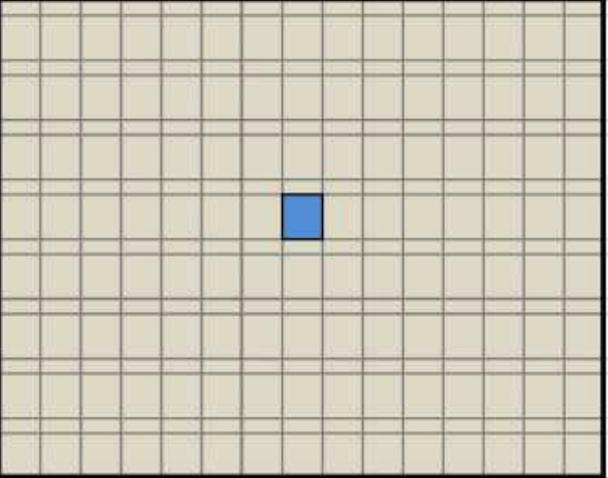
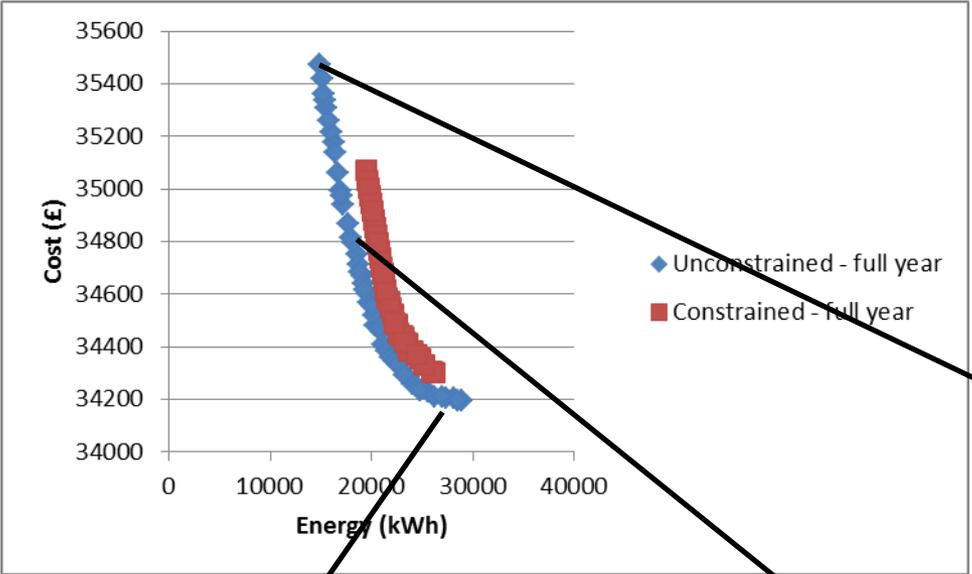
Energy Use



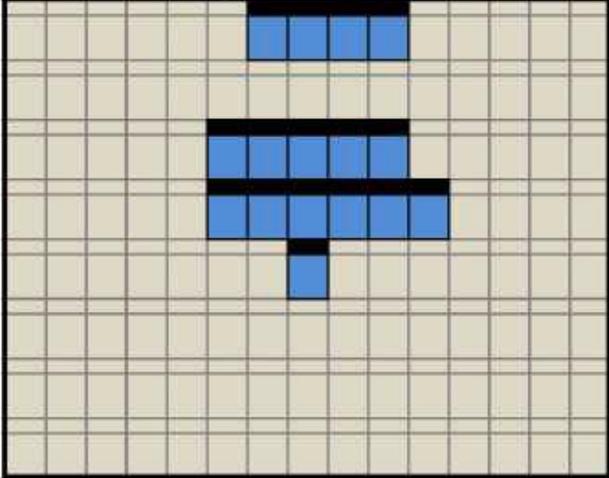




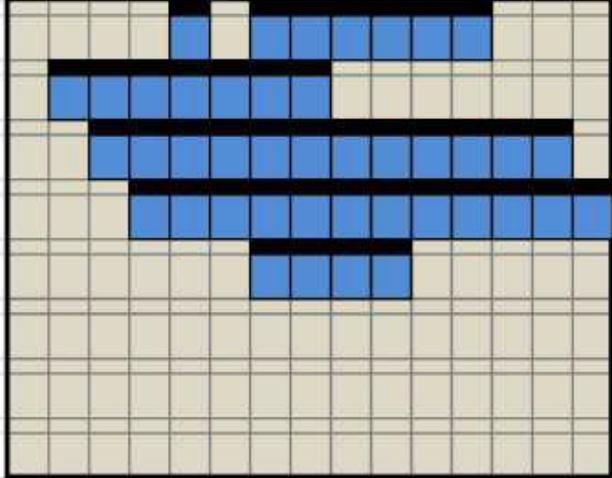
# Example 1: Cellular Windows



(a)  
Lowest capital cost;  
highest energy use



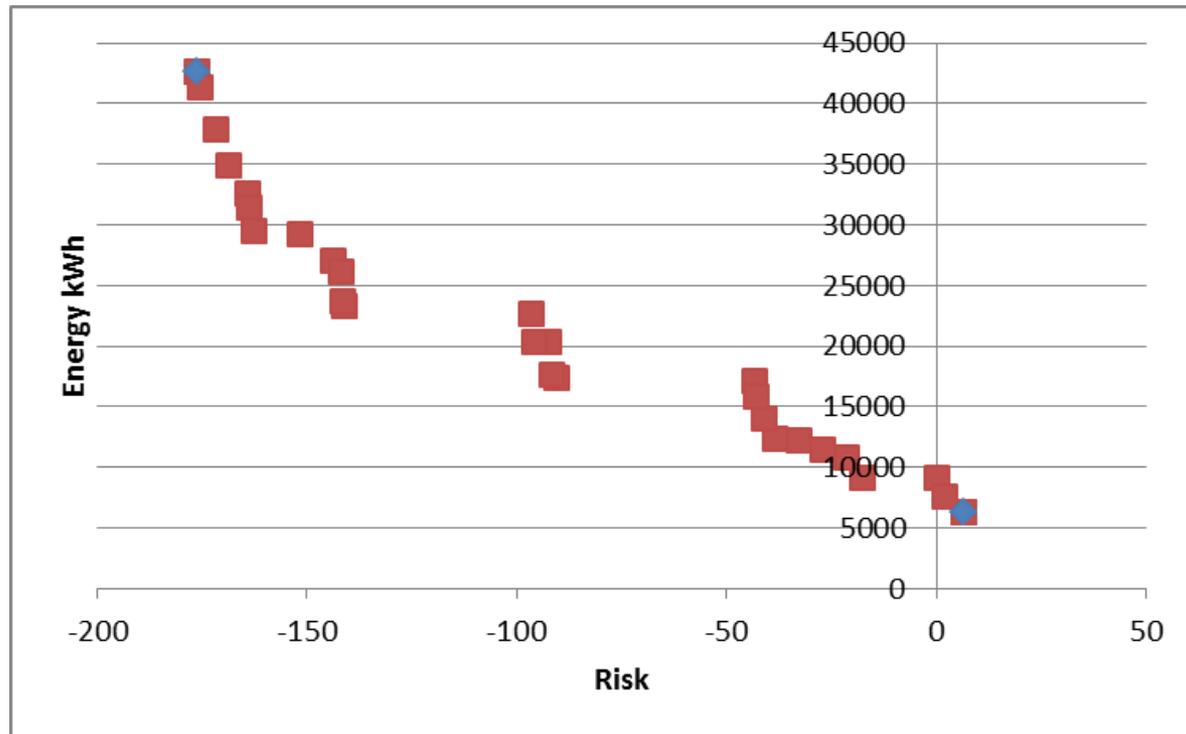
(b)  
Median capital cost  
and energy use



(c)  
Highest capital cost  
and lowest energy use

# Example 2: Risk of mould growth

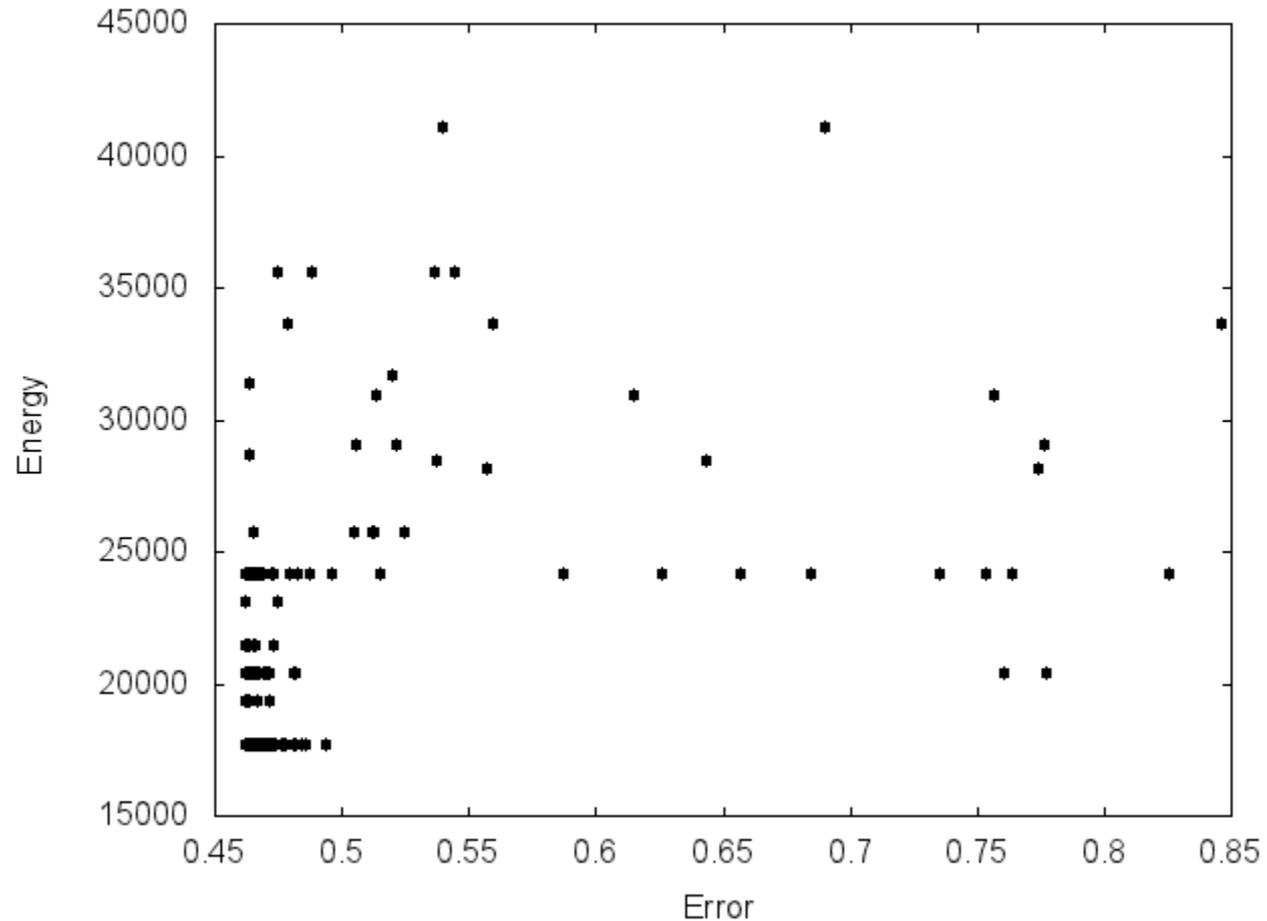
- Hospital ward in Kuala Lumpur
- Optimise air conditioning / ventilation configuration to identify high risk conditions
- Risk related to long, warm, damp periods



# Some other applications...

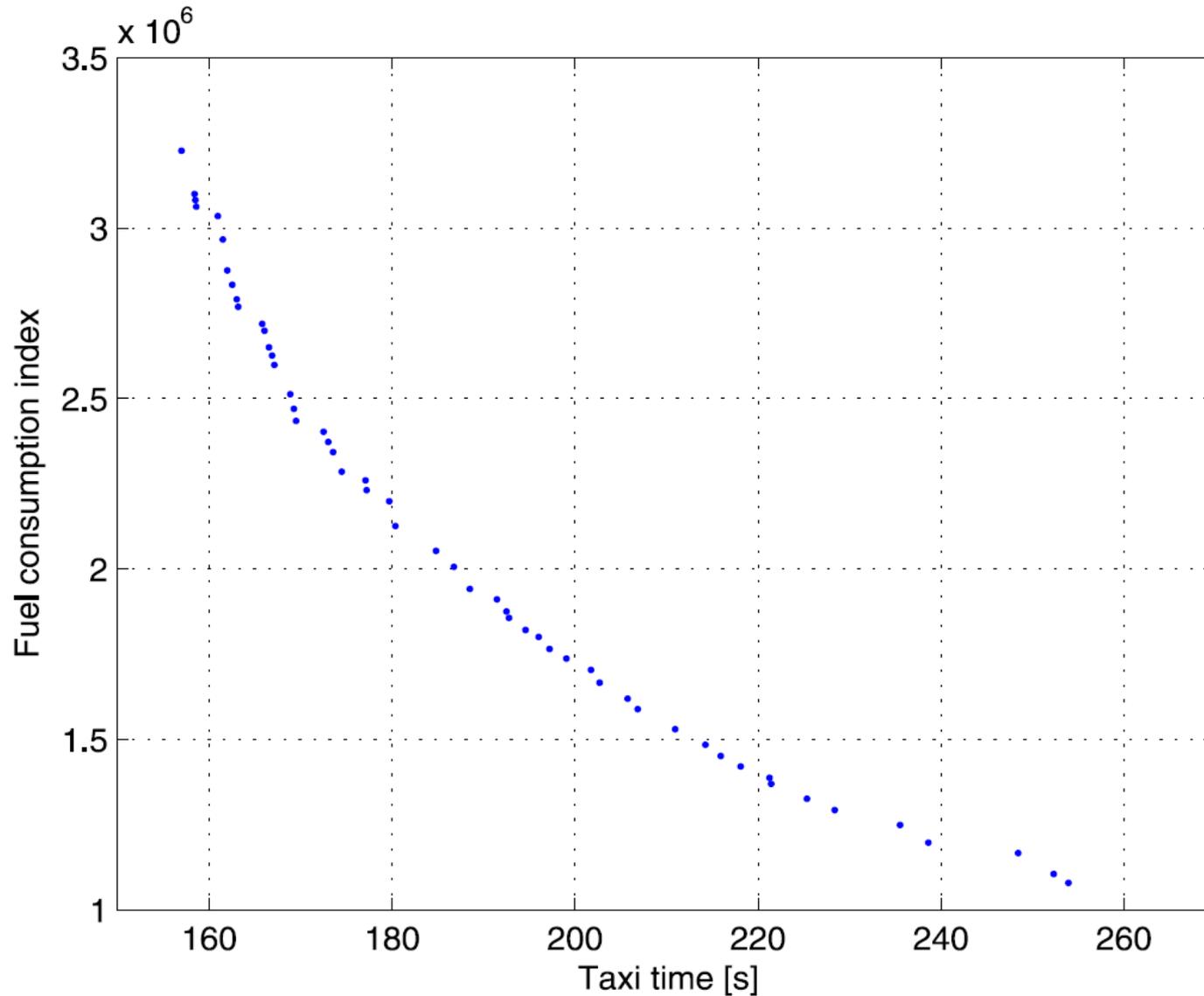
# More efficient software

- What's more important?
  - Run faster
  - Better results
  - Longer on battery
- More on ANNs
  - for associative memory
  - 12 May
  - Bruce Graham



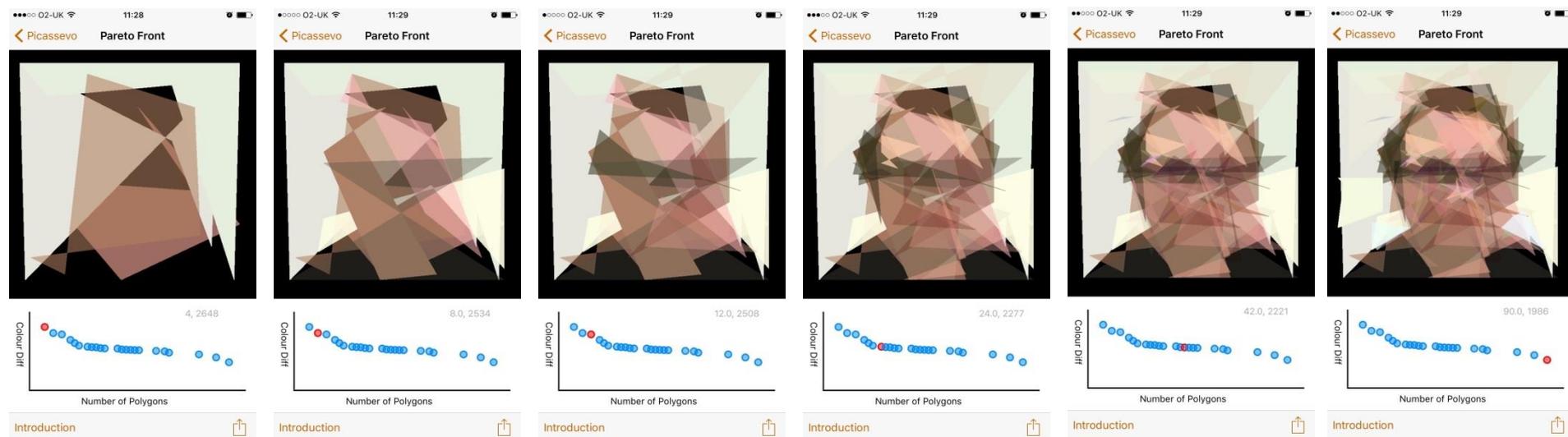
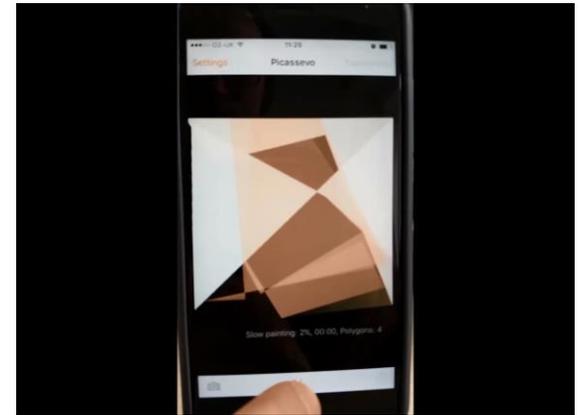


# Greener Aircraft Taxiing



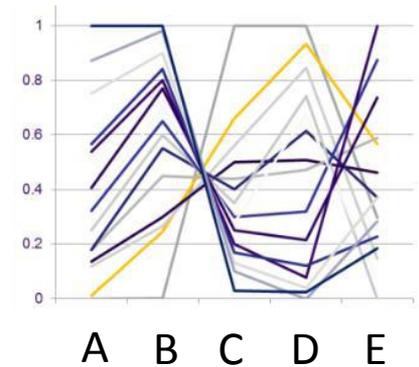
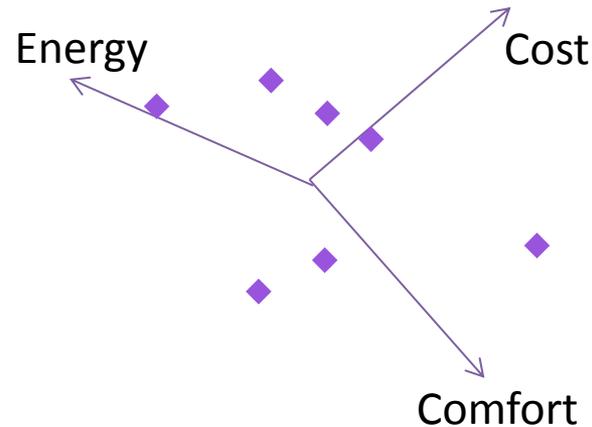
# Picassevo

- Free from the iPhone app store
- <https://appsto.re/gb/en1Nab.i>
- Developed by our partners in the DAASE project at UCL:
  - <http://daase.cs.ucl.ac.uk>



# Ongoing research

- many objectives
  - how to optimise?
  - how to visualise?



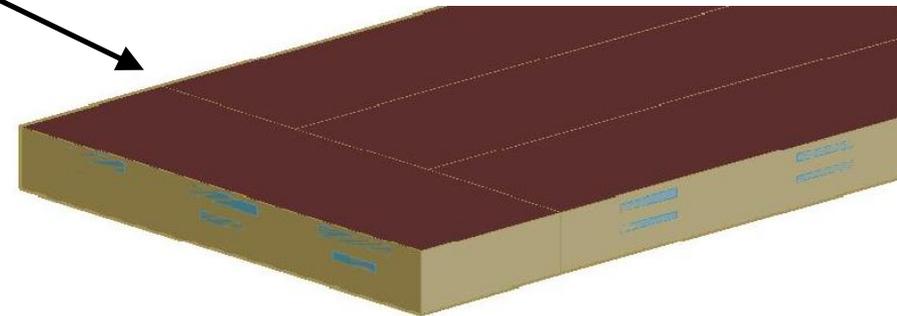
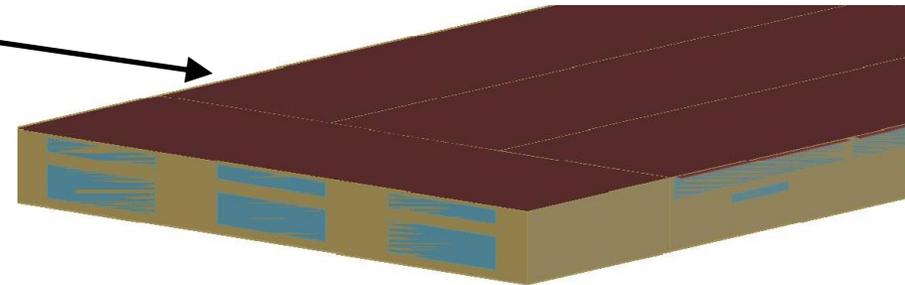
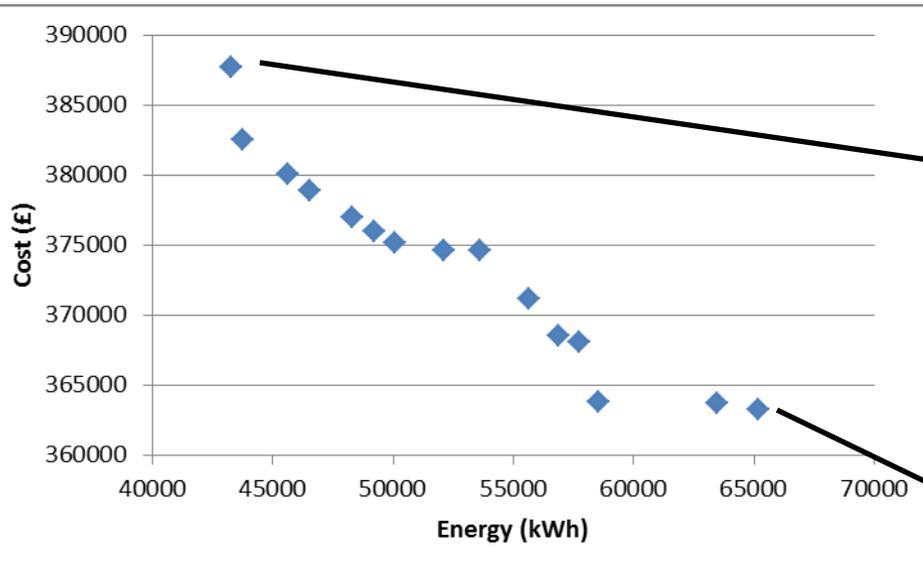
- exploring the Pareto front
- more efficient search methods
- human in the loop

# Thanks!

- [www.cs.stir.ac.uk/~sbr](http://www.cs.stir.ac.uk/~sbr) --- [sbr@cs.stir.ac.uk](mailto:sbr@cs.stir.ac.uk)
- Picassevo: <https://appsto.re/gb/en1Nab.i>
- Article on nature-inspired algorithms
  - "Why we fell out of love with algorithms inspired by nature" (link from homepage above)
- **Next Lecture: 31<sup>st</sup> March**
- **Zero: the history of an unappreciated number.**  
**Dr Anthony O'Hare**



# Example 3: Office building



# Exploring the Pareto front

- A – heating set point
- B – cooling set-point
- C – temp for nat. vent
- D – glazed area (N Upper)
- E – glazed area (S Upper)
- F – mech. ventilation rate
- G – external wall type
- H – ceiling and floor type
- I – shading overhang (S)

Energy	CapCost	A	B	C	D	E	F	G	H	I
0.00	1.00	0.5	0.564516	0.98	0.85	0.82	0.11	0	1	1
0.01	0.90	0.5	0.564516	0.98	0.85	0.79	0.11	0	1	1
0.03	0.82	0.5	0.580645	0.98	0.57	0.79	0.11	0	1	1
0.04	0.76	0.5	0.580645	0.98	0.49	0.79	0.11	0	1	0
0.07	0.74	0.5	0.564516	0.98	0.49	0.79	0.11	0	1	0
0.07	0.70	0.5	0.564516	0.98	0.49	0.79	0.22	0	1	0
0.10	0.66	0.5	0.580645	0.98	0.41	0.79	0.11	0	1	0
0.10	0.62	0.5	0.564516	0.98	0.85	0.82	1.00	1	1	1
0.10	0.61	0.5	0.564516	0.98	0.85	0.82	0.11	1	1	1
0.10	0.61	0.5	0.564516	0.98	0.85	0.82	1.00	1	1	1
0.12	0.59	0.5	0.612903	0.98	0.85	0.82	0.67	1	1	1
0.14	0.57	0.5	0.548387	0.98	0.49	0.79	0.11	1	1	0
0.15	0.54	0.4	0.548387	0.98	0.57	0.79	0.67	1	1	0
0.17	0.53	0.4	0.548387	0.98	0.57	0.79	0.67	1	1	0
0.18	0.52	0.5	0.564516	0.98	0.49	0.79	0.11	1	1	0
0.18	0.49	0.4	0.548387	0.98	0.57	0.79	0.67	1	1	0
0.21	0.45	0.4	0.564516	0.98	0.41	0.43	0.11	0.5	1	0
0.21	0.43	0.5	0.564516	0.98	0.57	0.43	0.67	1	1	0
0.21	0.37	0.4	0.548387	0.98	0.49	0.43	0.67	1	1	0
0.24	0.35	0.4	0.548387	0.98	0.49	0.43	0.67	1	1	0
0.27	0.32	0.4	0.548387	0.98	0.41	0.43	0.11	1	1	0
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0.35	0.27	0.4	0.580645	0.98	0.35	0.43	0.11	1	1	0
0.35	0.26	0.4	0.596774	0.98	0.24	0.43	0.11	1	1	0
0.36	0.25	0.4	0.548387	0.98	0.29	0.43	0.11	1	1	0
0.38	0.25	0.4	0.596774	0.98	0.33	0.33	0.11	1	1	0
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0.49	0.18	0.4	0.596774	0.98	0.24	0.33	1.00	1	1	0
0.54	0.16	0.4	0.532238	1.00	0.24	0.33	0.11	1	1	0
0.55	0.14	0.4	0.596774	0.98	0.24	0.33	0.67	1	1	0
0.57	0.12	0.4	0.596774	0.98	0.24	0.33	0.11	1	1	0
0.64	0.11	0.4	0.612903	0.98	0.24	0.43	0.11	1	1	0
0.64	0.11	0.4	0.612903	0.98	0.33	0.33	0.00	1	1	0
0.65	0.09	0.4	0.596774	0.98	0.24	0.33	0.11	1	1	0
0.66	0.08	0.4	0.612903	0.98	0.24	0.33	0.11	1	1	0
0.67	0.08	0.4	0.612903	0.98	0.24	0.33	0.11	1	1	0
0.67	0.07	0.4	0.612903	0.98	0.24	0.33	0.11	1	1	0
0.70	0.07	0.4	0.612903	1.00	0.24	0.33	0.11	1	1	0
0.91	0.05	0.4	0.612903	0.98	0.33	0.04	0.11	1	1	0
0.91	0.04	0.4	0.596774	0.98	0.33	0.04	0.11	1	1	0
0.91	0.01	0.4	0.596774	0.98	0.29	0.04	0.11	1	1	0
0.97	0.01	0.4	0.612903	0.98	0.24	0.04	0.11	1	1	0
1.00	0.00	0.4	0.612903	1.00	0.24	0.04	0.11	1	1	0
Corr. with energy:		-0.76	0.63	0.32	-0.86	-0.93	-0.31	0.61	0.00	-0.54